

LEBT Beam Focusing Simulations

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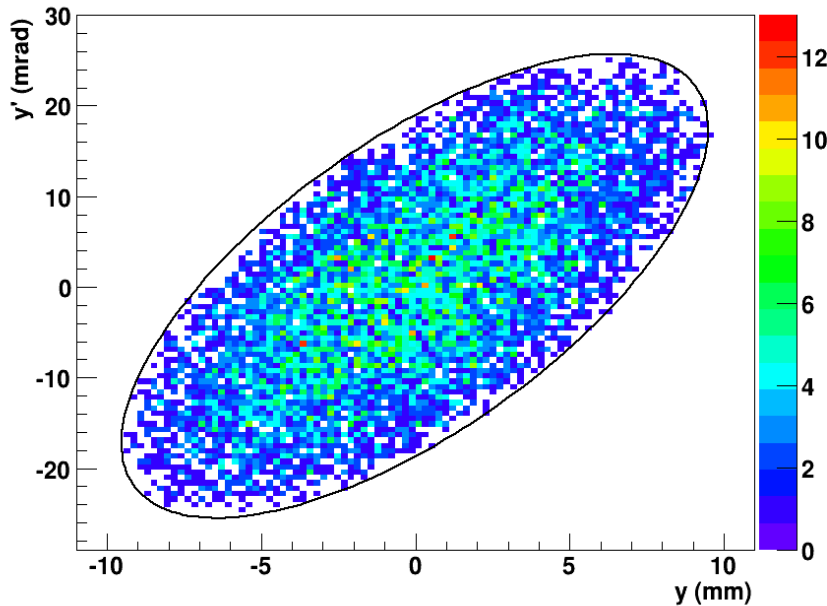
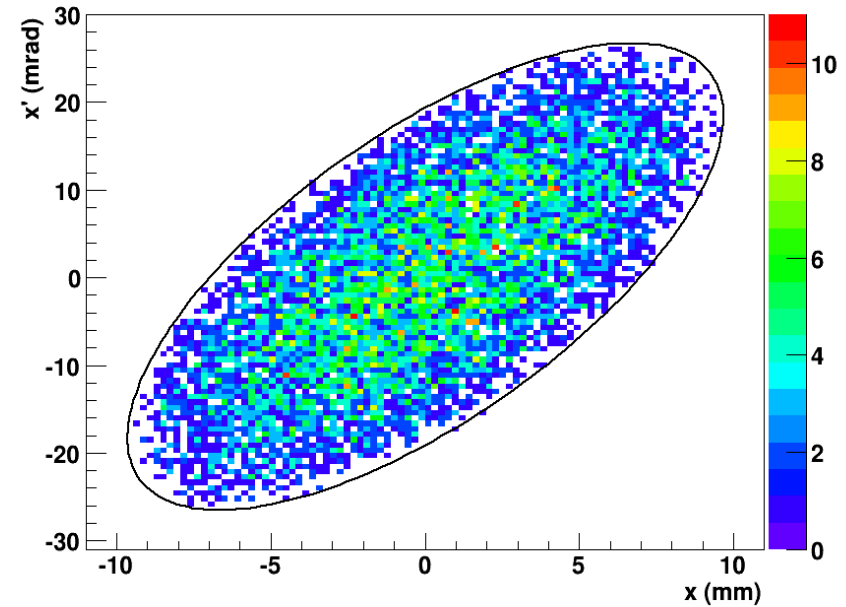
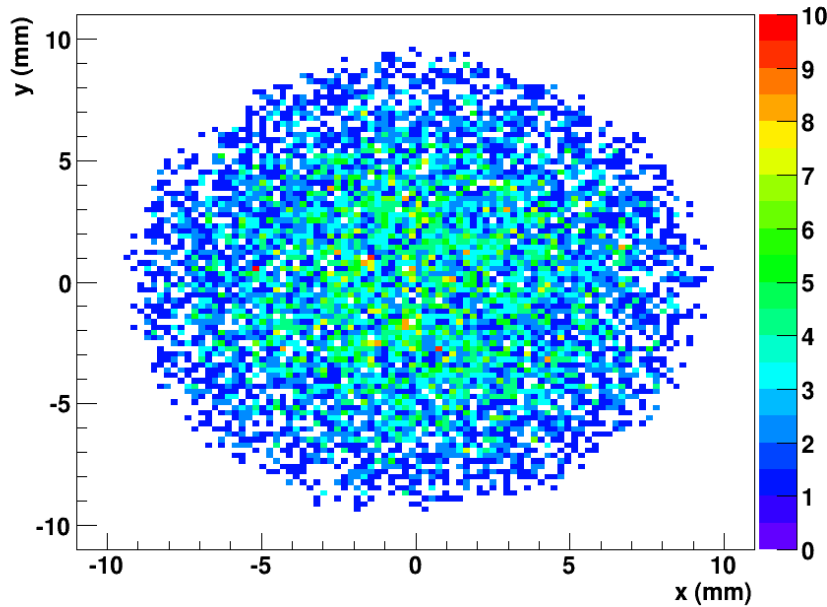
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Introduction

- GPT simulations of LEBT beam focusing
 - 65 keV beam, 5 mA space charge, 10k events
 - initial beam Twiss parameters from (old) pepperpot data
- Systematic variation of (the 3) solenoid currents
 - Investigate allowed current ranges to get optimal beam focusing for RFQ acceptance
 - Choose I_1 , vary I_2 and I_3 in 10 A steps ($I_{\max} = 250$ A)
 - Focal length = final drift length where beam fraction inside RFQ acceptance ellipse is largest
 - Other drift lengths kept fixed ($d_1 = 21.7\text{cm}$, $d_2 = 15\text{cm}$, $d_3 = 35\text{cm}$)
- 2D histograms for main results:
 - RFQ fraction & focal length as a function of I_3 vs I_2 for given I_1

Assumed initial beam distribution

I1 = 137.0, I2 = 123.0, I3 = 216.0; d1 = 21.7, d2 = 15.0, d3 = 35.0; KE = 65.0 keV



Region = Start

$\langle x \rangle = 0.02 \text{ mm}$, $\langle x' \rangle = 0.08 \text{ mrad}$

$\langle y \rangle = -0.02 \text{ mm}$, $\langle y' \rangle = 0.10 \text{ mrad}$

$\alpha_x = -0.96$, $\beta_x = 0.50$, $\gamma_x = 3.82$; $(1 + \alpha_x^2)/\beta_x = 3.82$

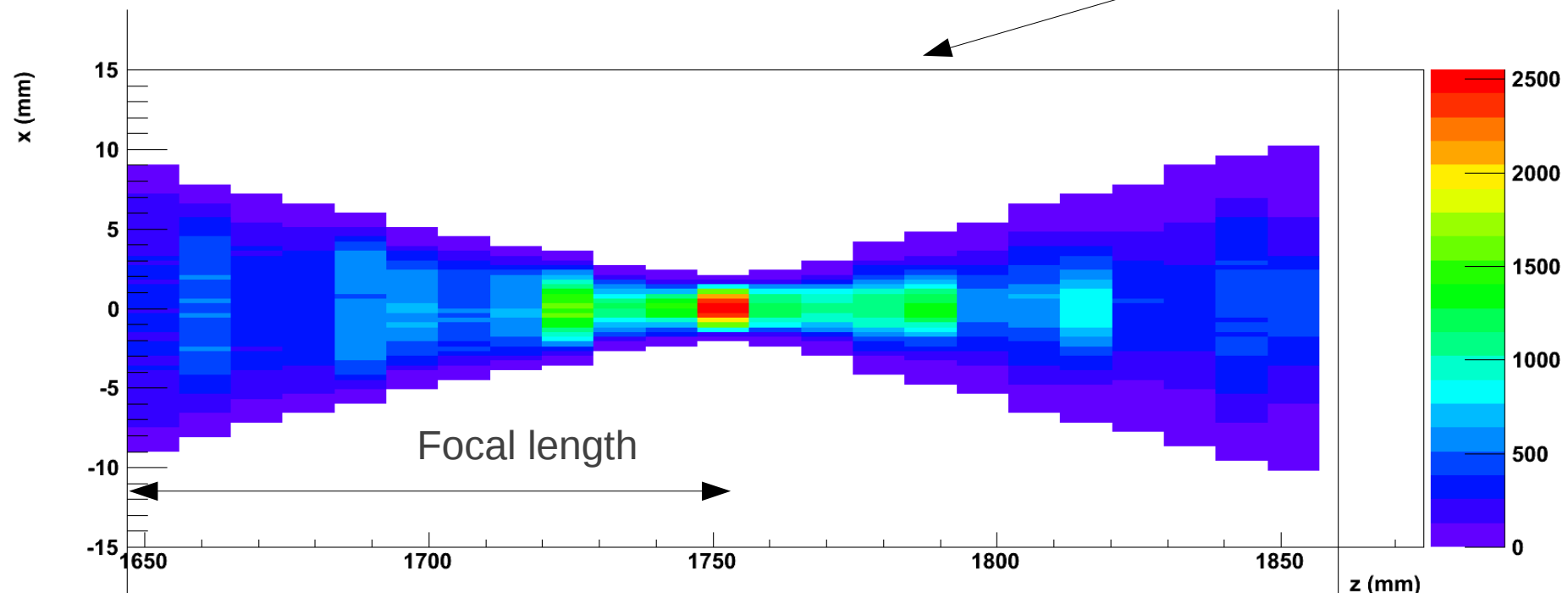
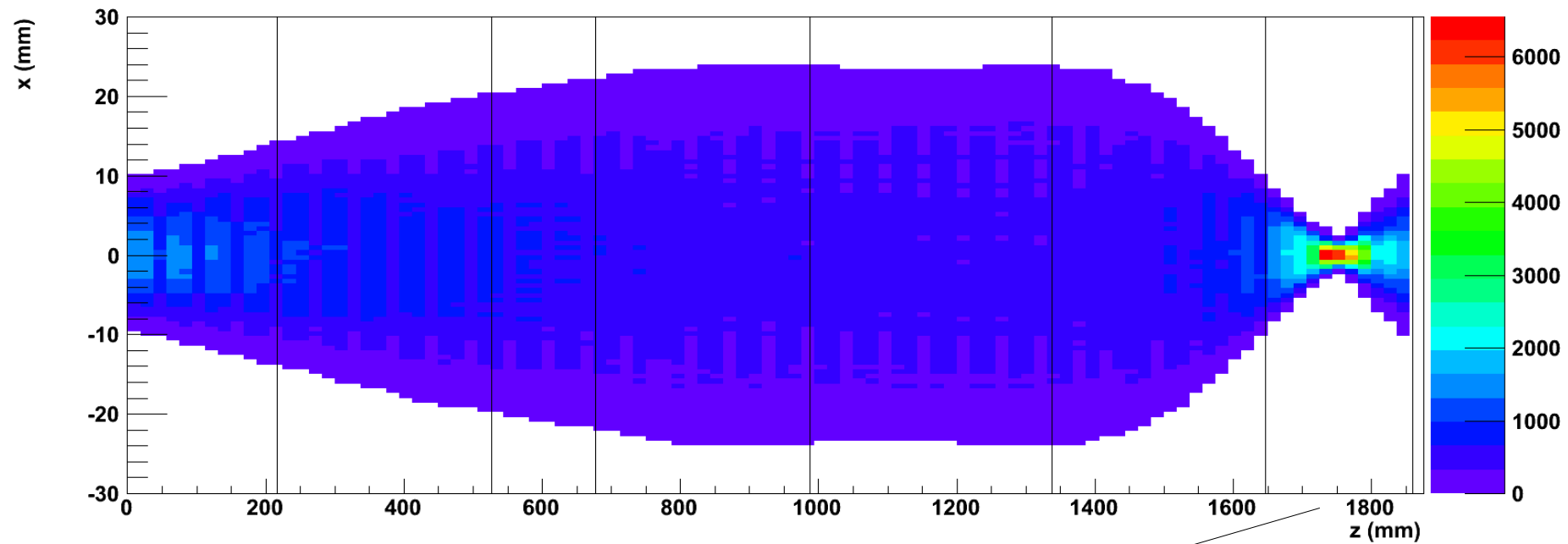
$\alpha_y = -0.92$, $\beta_y = 0.50$, $\gamma_y = 3.66$; $(1 + \alpha_y^2)/\beta_y = 3.66$

$\epsilon_x = 185.78$, Norm $\epsilon_x = 2.19$, Norm rms $\epsilon_x = 0.36$

$\epsilon_y = 179.15$, Norm $\epsilon_y = 2.11$, Norm rms $\epsilon_y = 0.35$

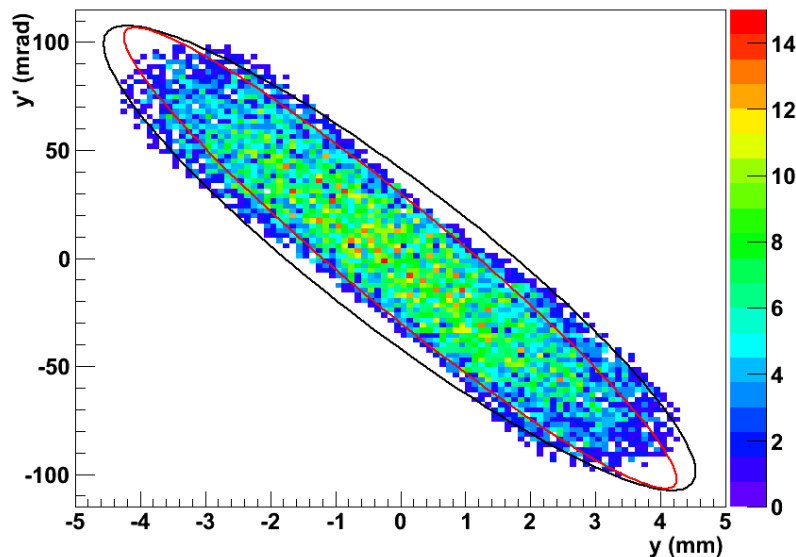
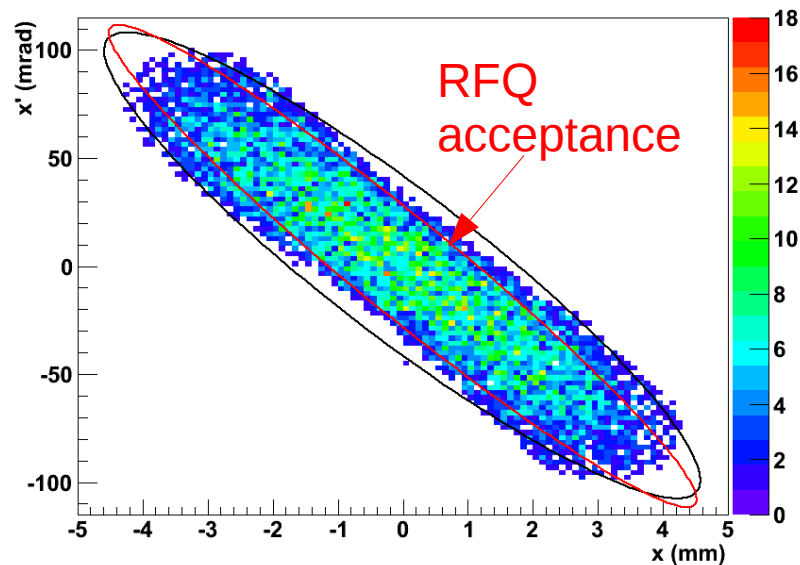
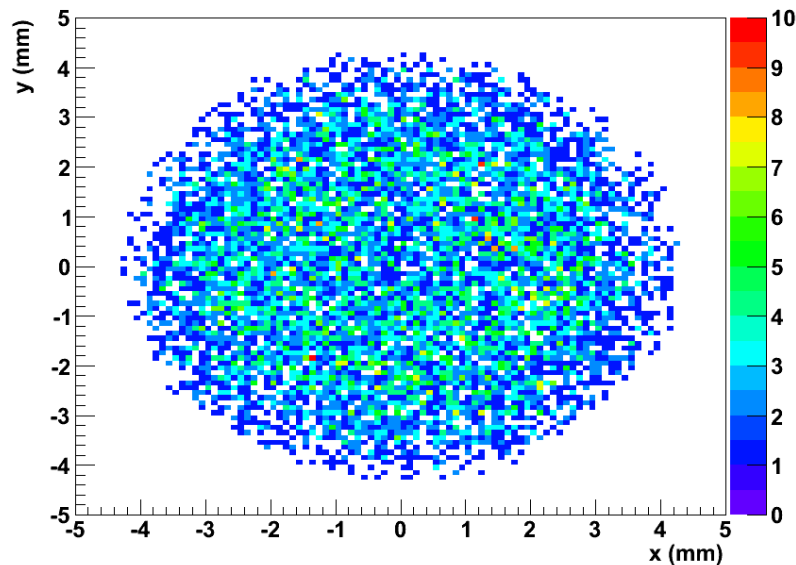
Example beam x-z envelope

$I_1 = 100.0$, $I_2 = 100.0$, $I_3 = 230.0$; $d_1 = 21.7$, $d_2 = 15.0$, $d_3 = 35.0$; $KE = 65.0$ keV



Example “optimal” beam emittance at end of LEBT

I1 = 100.0, I2 = 100.0, I3 = 230.0; d1 = 21.7, d2 = 15.0, d3 = 35.0; KE = 65.0 keV



Region = 60 mm from start of drift 4

$\langle x \rangle = -0.01$ mm, $\langle x' \rangle = 0.35$ mrad

$\langle y \rangle = -0.01$ mm, $\langle y' \rangle = 0.02$ mrad

$\alpha_x = 2.39$, $\beta_x = 0.11$, $\gamma_x = 60.93$; $(1 + \alpha_x^2)/\beta_x = 60.93$

$\alpha_y = 2.36$, $\beta_y = 0.11$, $\gamma_y = 60.71$; $(1 + \alpha_y^2)/\beta_y = 60.71$

$\epsilon_x = 190.86$, Norm $\epsilon_x = 2.25$, Norm rms $\epsilon_x = 0.37$

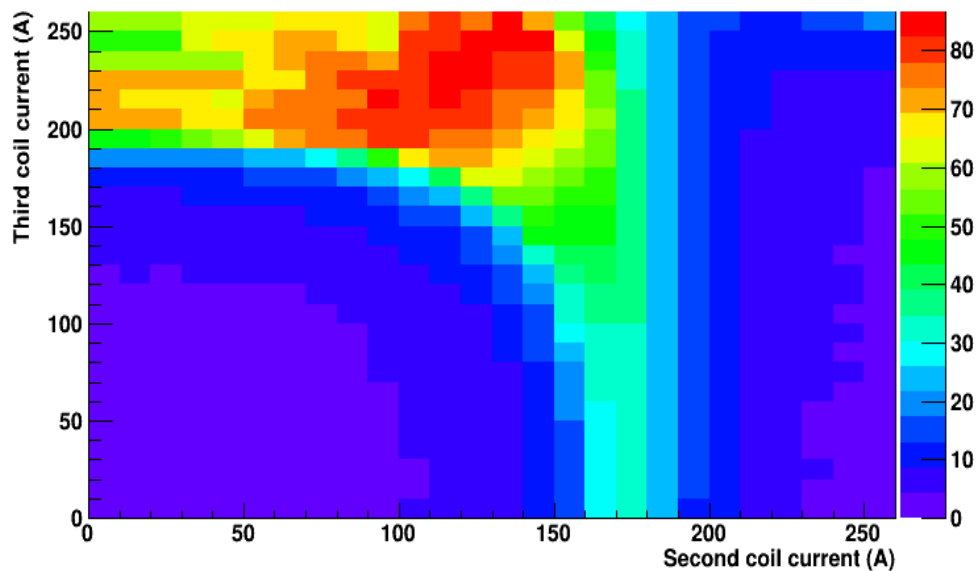
$\epsilon_y = 190.32$, Norm $\epsilon_y = 2.24$, Norm rms $\epsilon_y = 0.37$

RFQ x fraction = 83.16 %, y fraction = 85.30 %

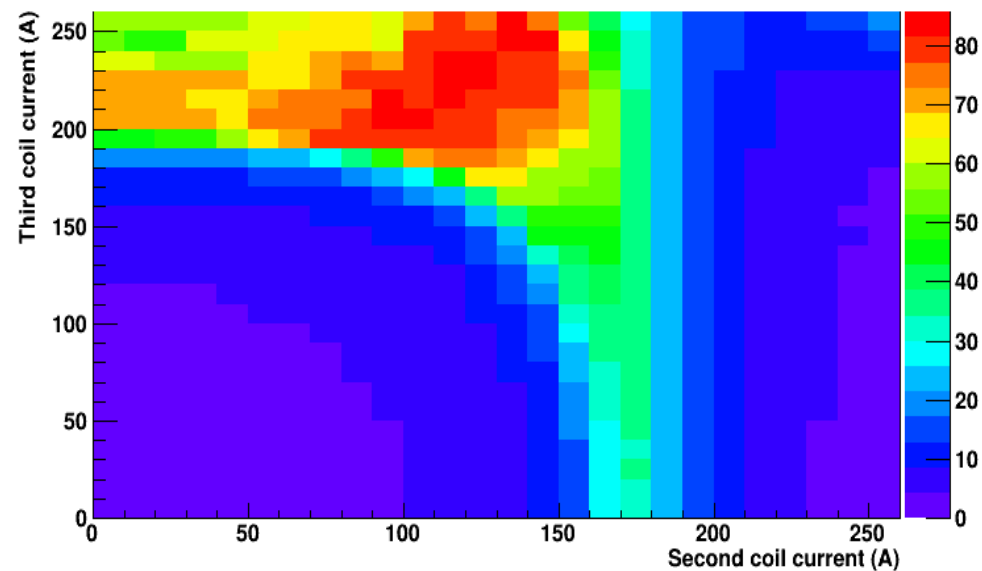
Max RFQ fraction

$$I_1 = 0 \text{ A}$$

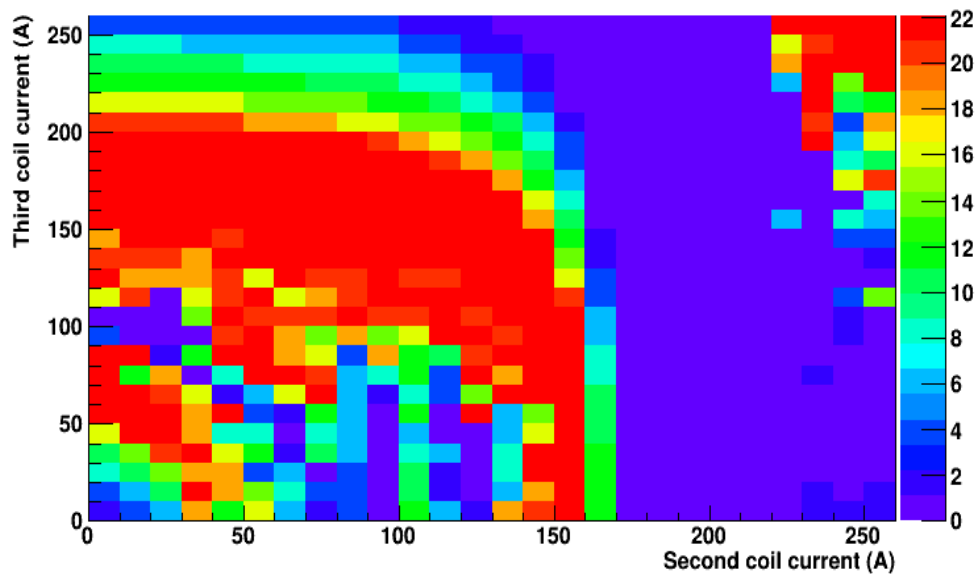
Maximum RFQ x-x' acceptance (%)



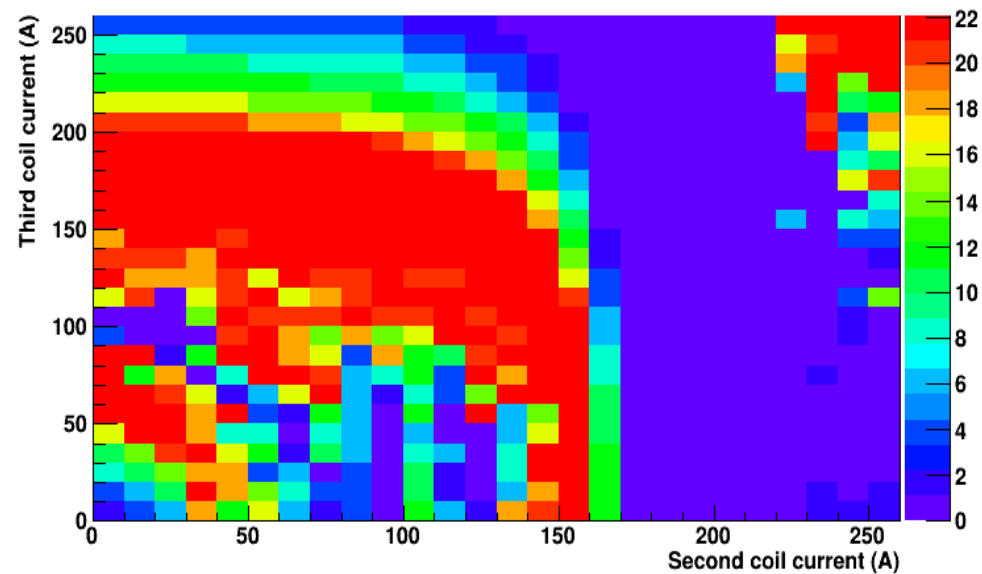
Maximum RFQ y-y' acceptance (%)



Final drift length (cm) at maximum x-x' RFQ acceptance

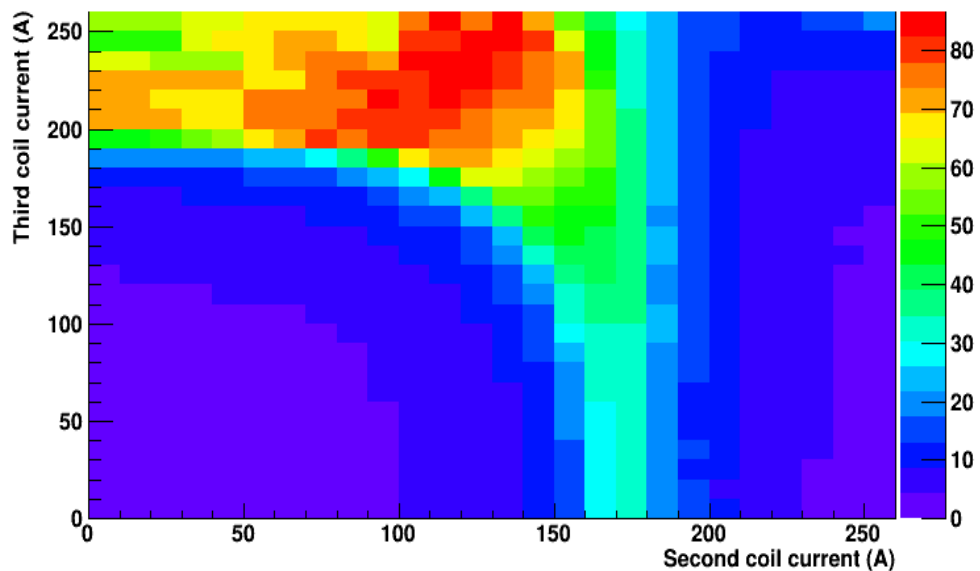


Final drift length (cm) at maximum y-y' RFQ acceptance

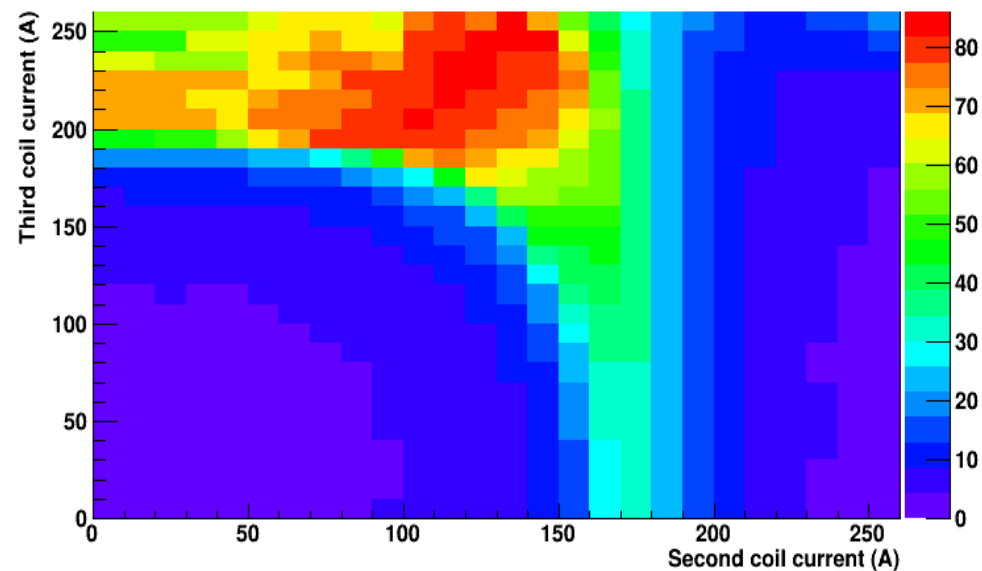


$$I_1 = 25 \text{ A}$$

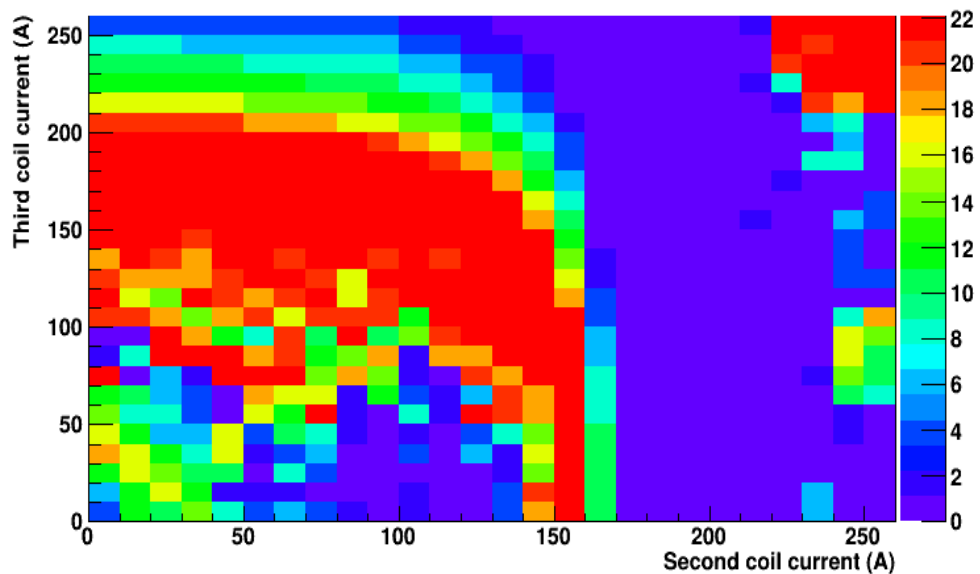
Maximum RFQ x-x' acceptance (%)



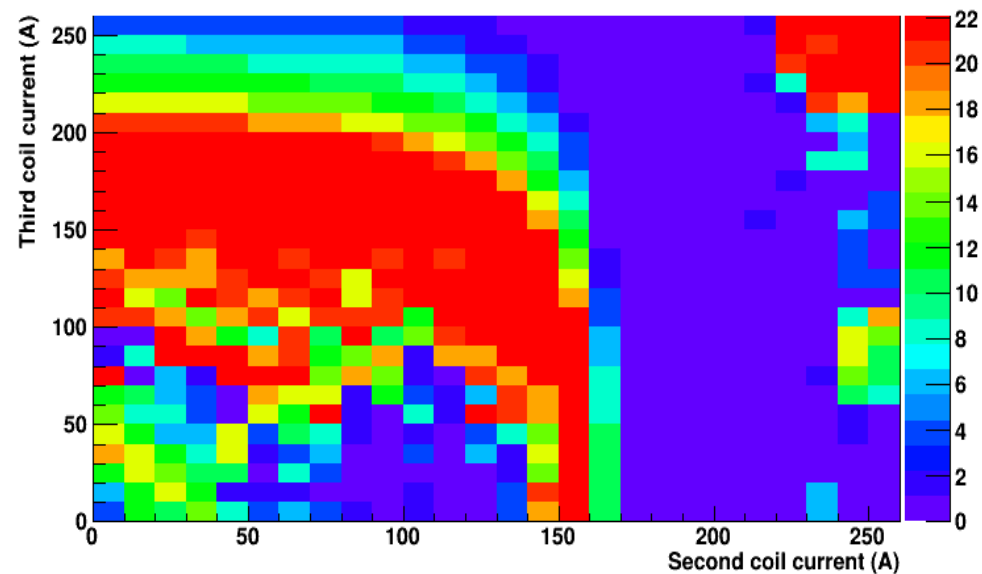
Maximum RFQ y-y' acceptance (%)



Final drift length (cm) at maximum x-x' RFQ acceptance

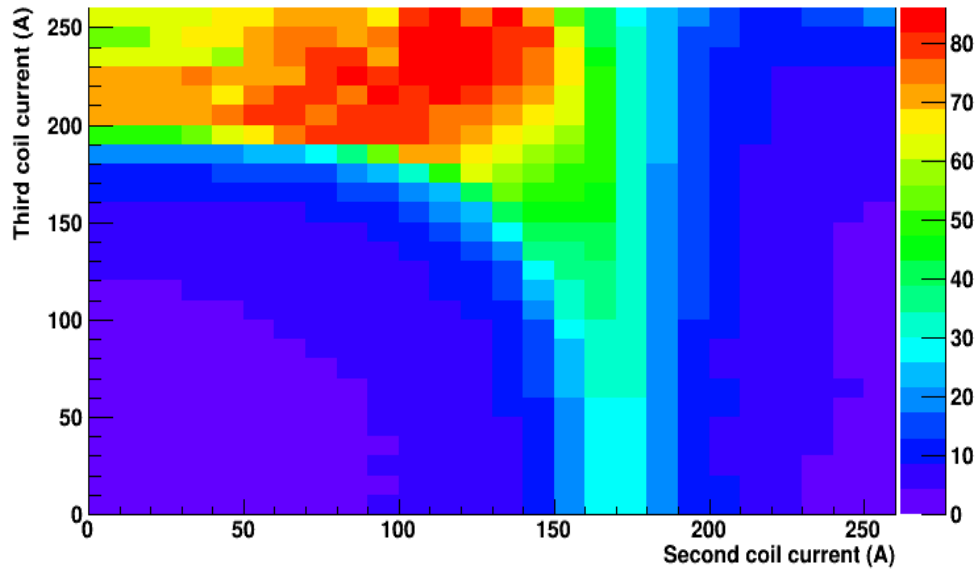


Final drift length (cm) at maximum y-y' RFQ acceptance

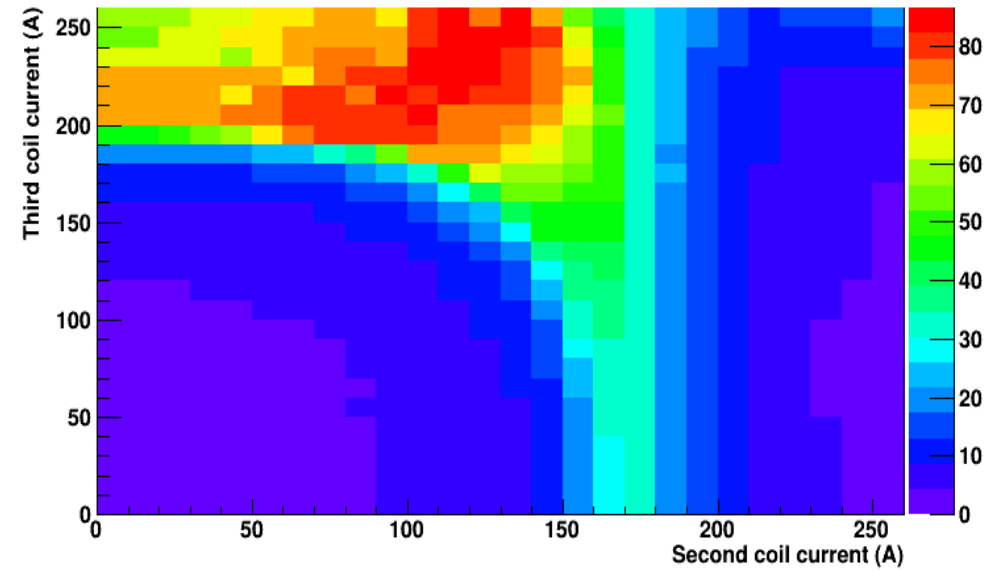


$$I_1 = 50 \text{ A}$$

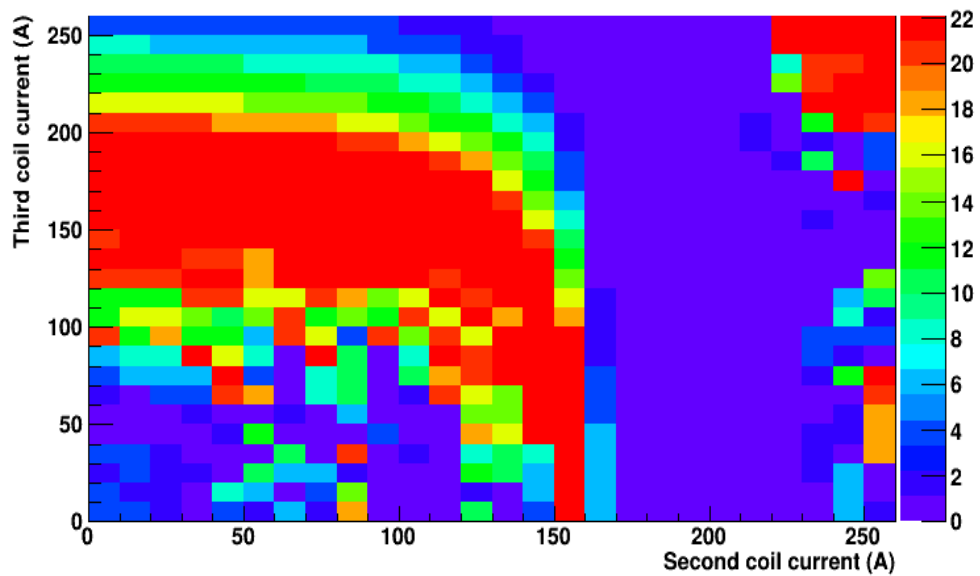
Maximum RFQ x-x' acceptance (%)



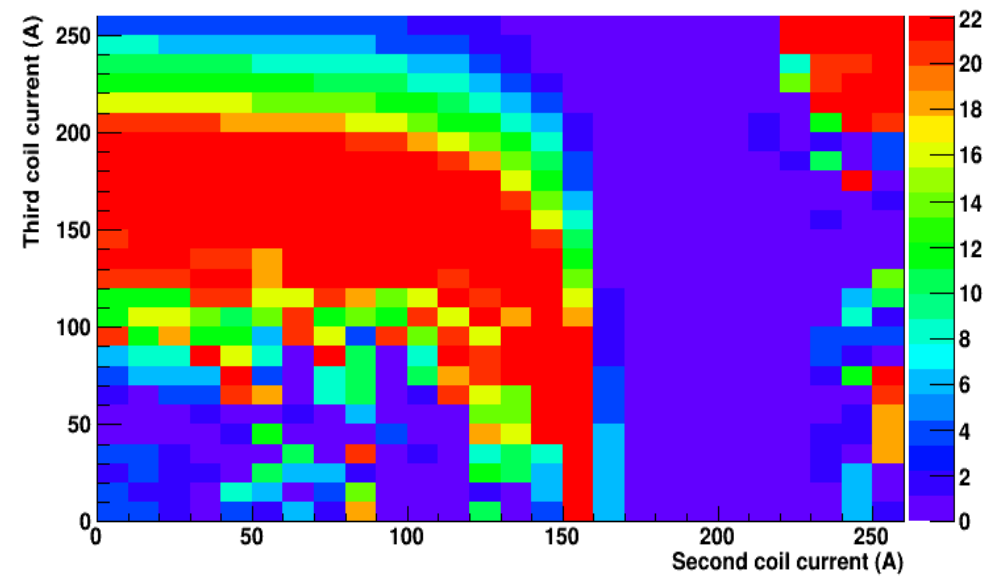
Maximum RFQ y-y' acceptance (%)



Final drift length (cm) at maximum x-x' RFQ acceptance

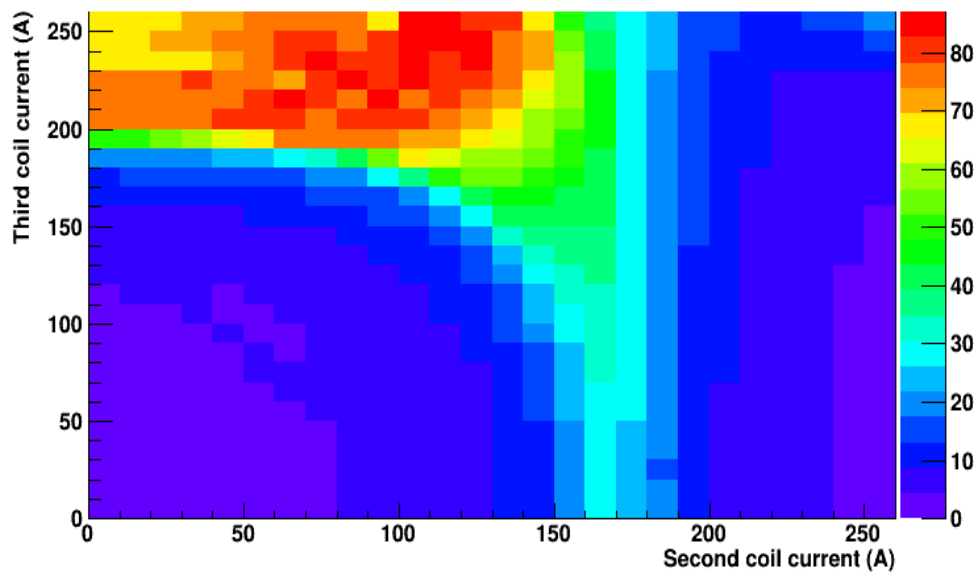


Final drift length (cm) at maximum y-y' RFQ acceptance

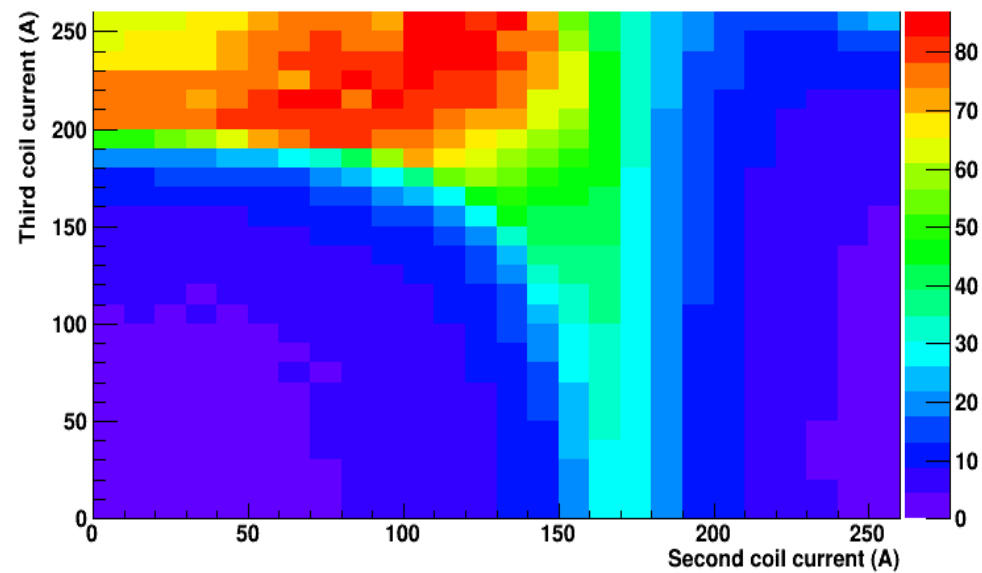


$$I_1 = 75 \text{ A}$$

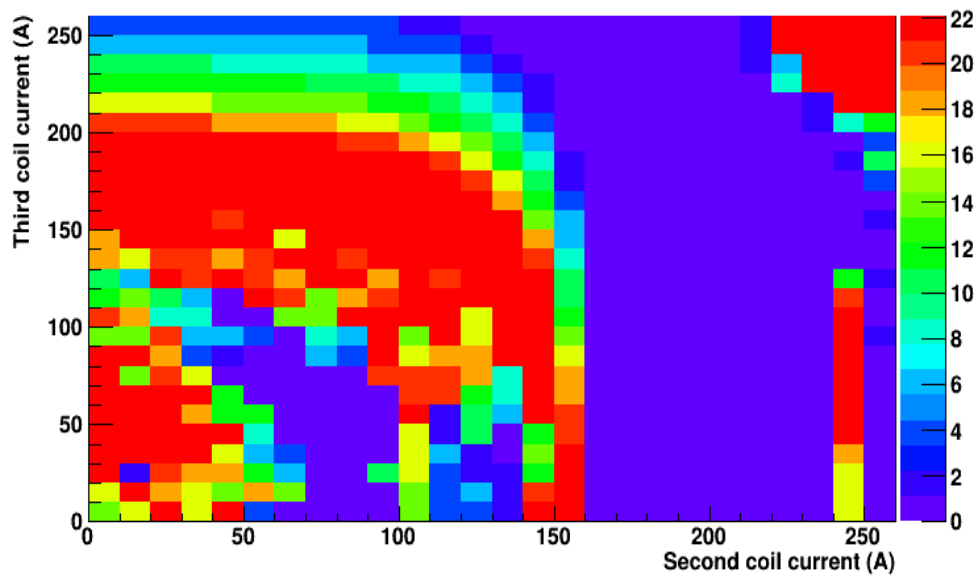
Maximum RFQ x-x' acceptance (%)



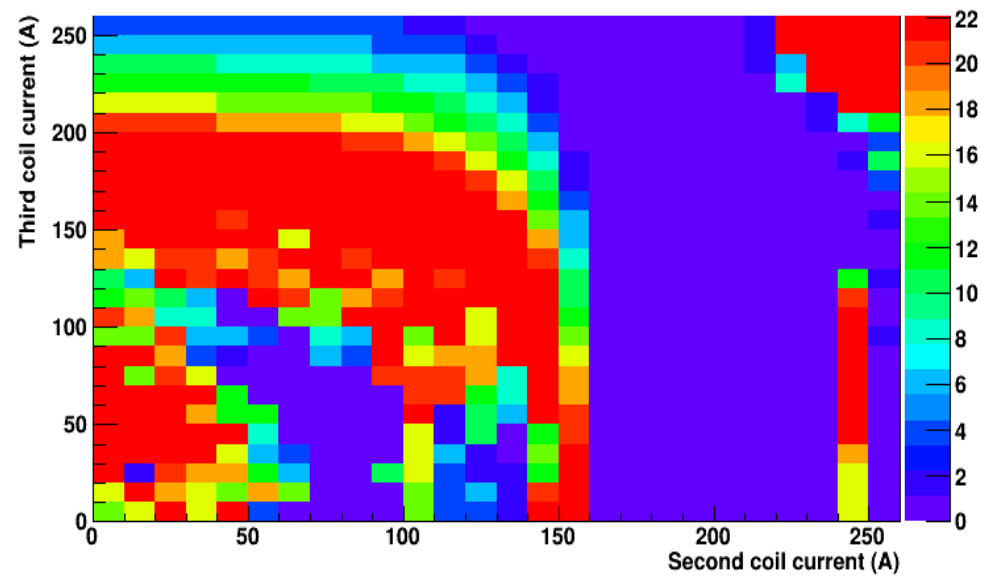
Maximum RFQ y-y' acceptance (%)



Final drift length (cm) at maximum x-x' RFQ acceptance

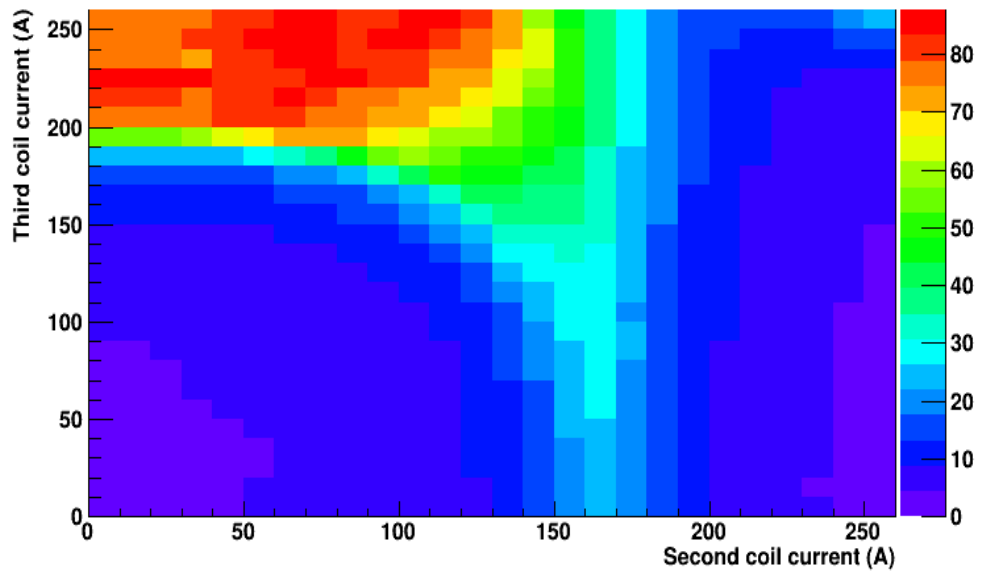


Final drift length (cm) at maximum y-y' RFQ acceptance

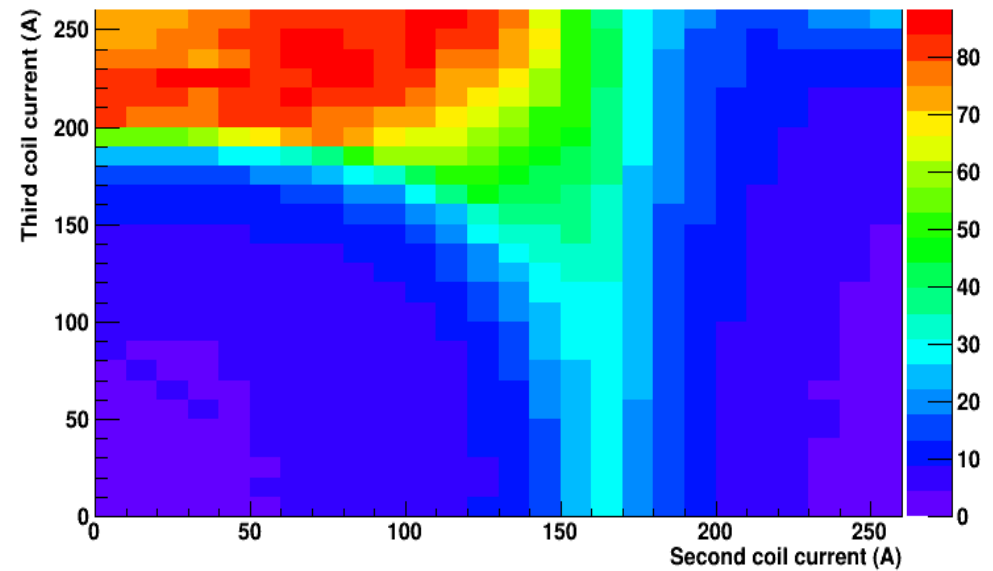


$$I_1 = 100 \text{ A}$$

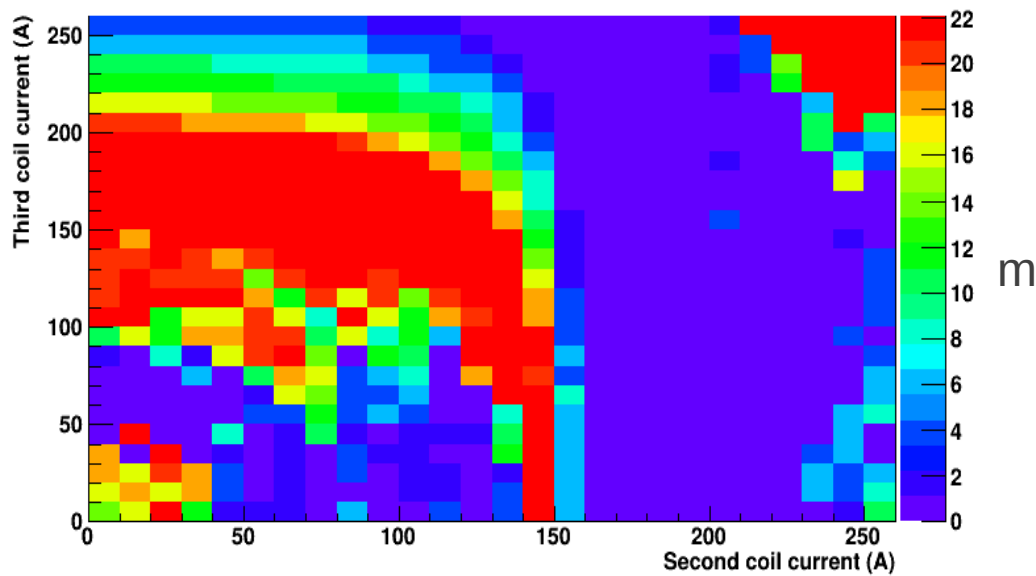
Maximum RFQ x-x' acceptance (%)



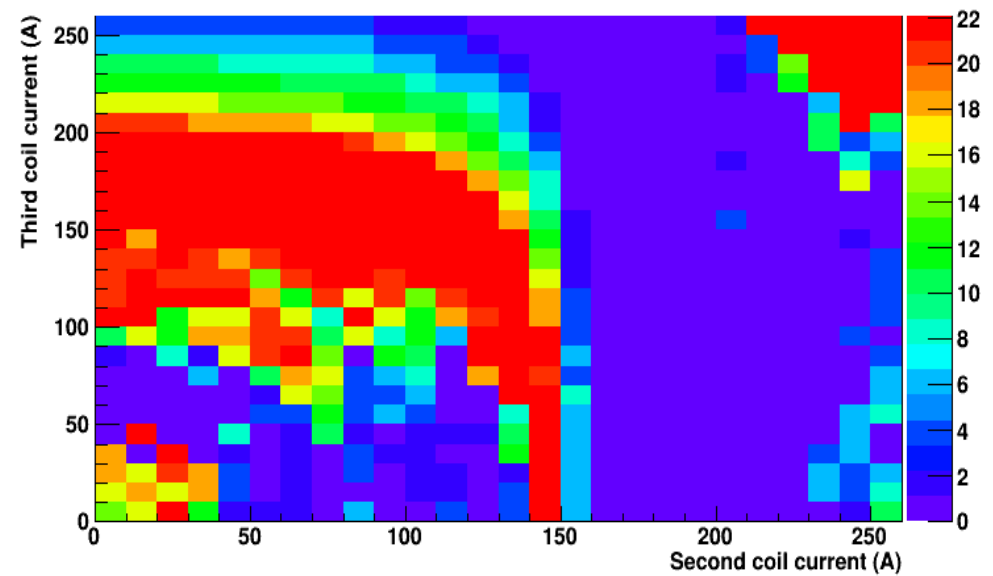
Maximum RFQ y-y' acceptance (%)



Final drift length (cm) at maximum x-x' RFQ acceptance



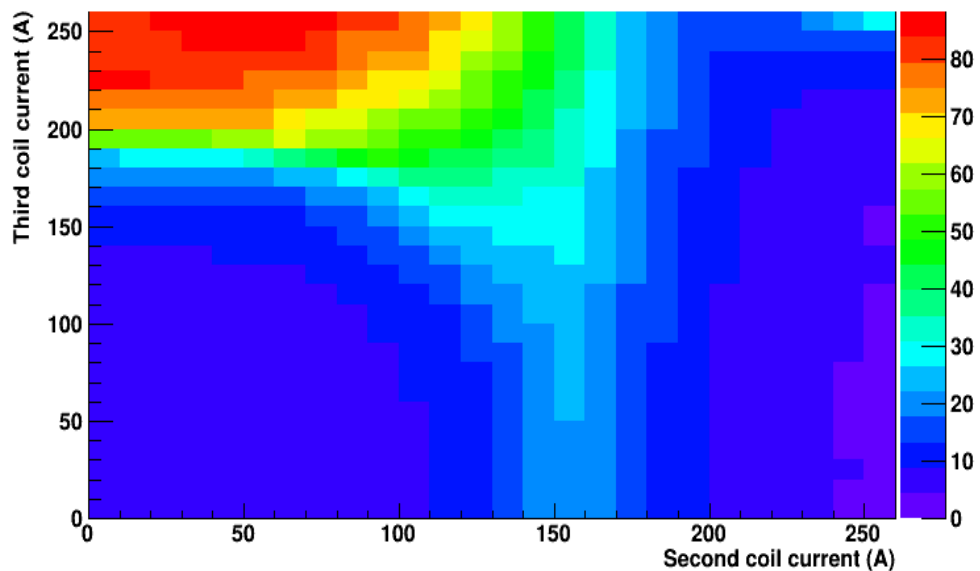
Final drift length (cm) at maximum y-y' RFQ acceptance



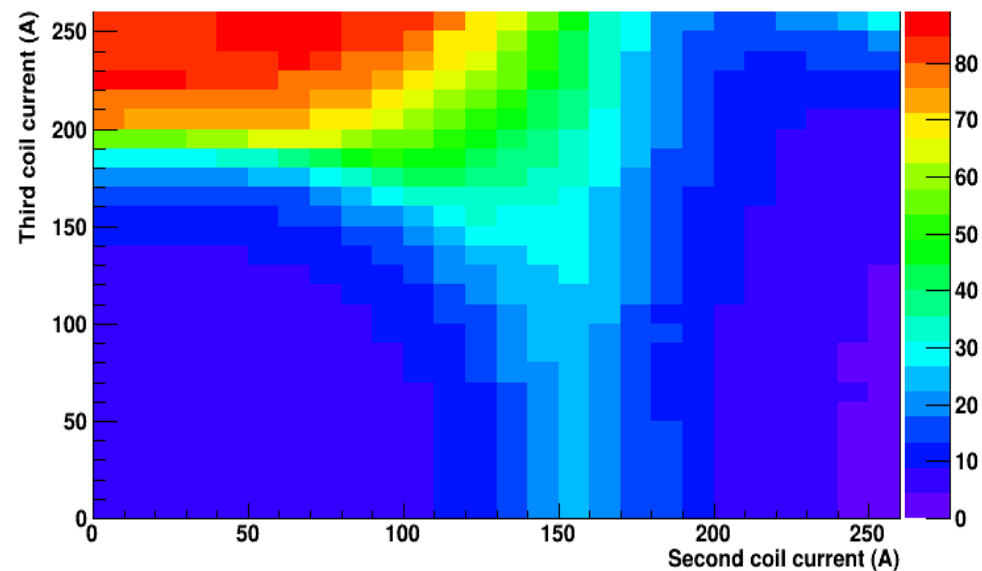
m

$$I_1 = 125 \text{ A}$$

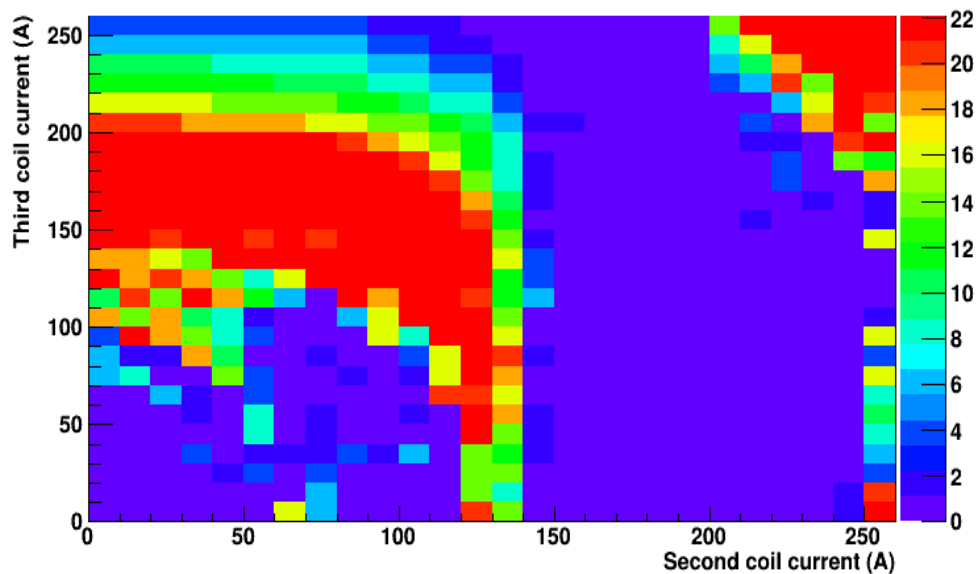
Maximum RFQ x-x' acceptance (%)



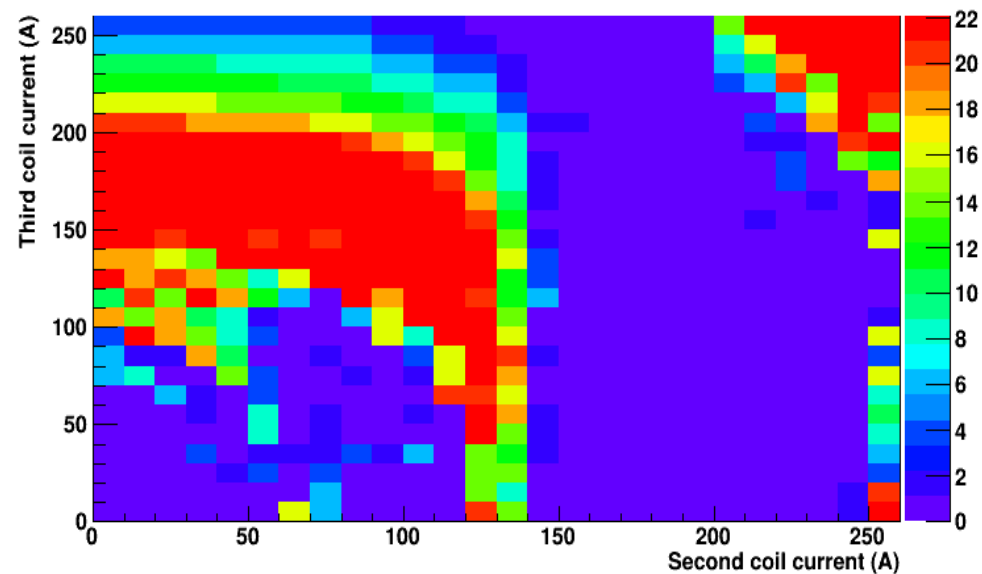
Maximum RFQ y-y' acceptance (%)



Final drift length (cm) at maximum x-x' RFQ acceptance

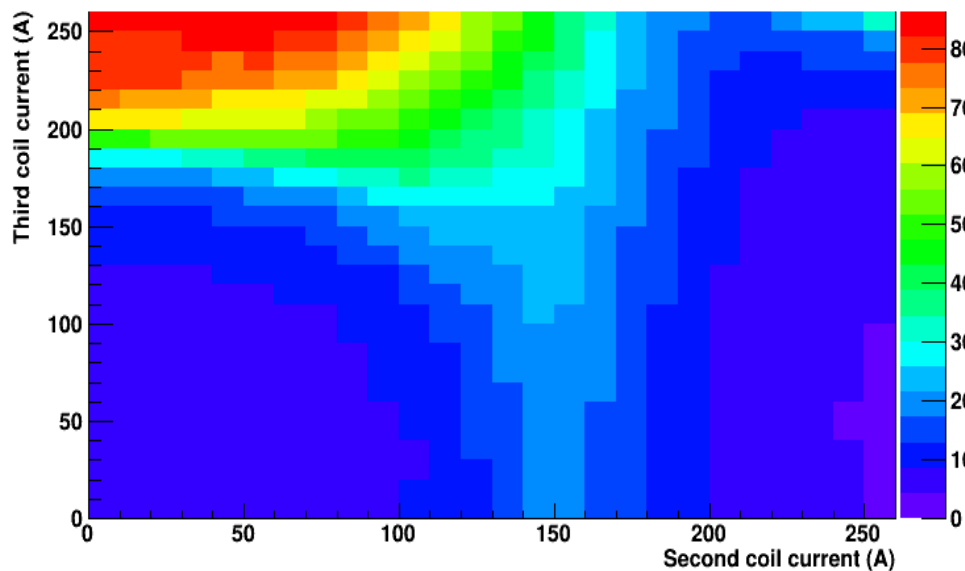


Final drift length (cm) at maximum y-y' RFQ acceptance

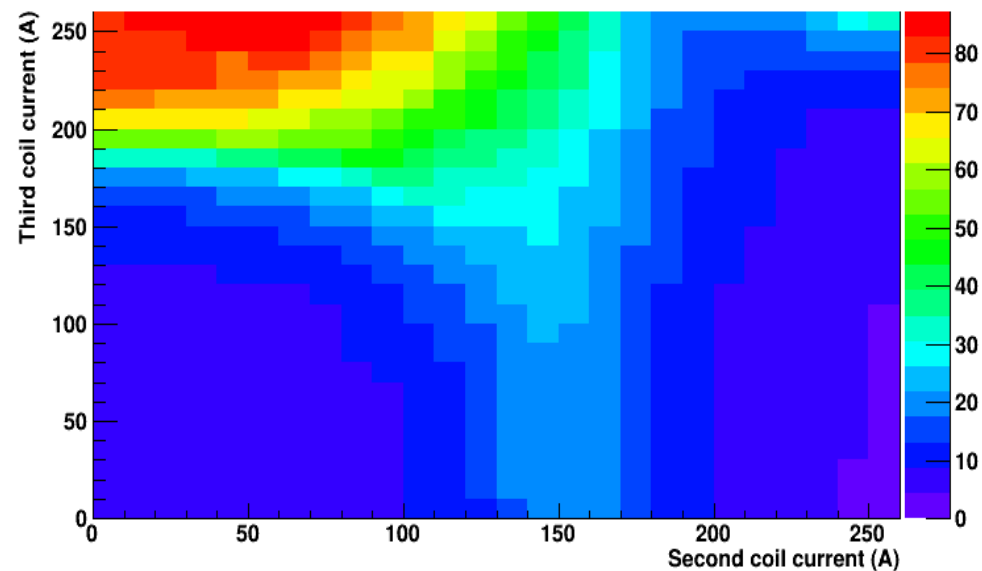


$$I_1 = 137 \text{ A}$$

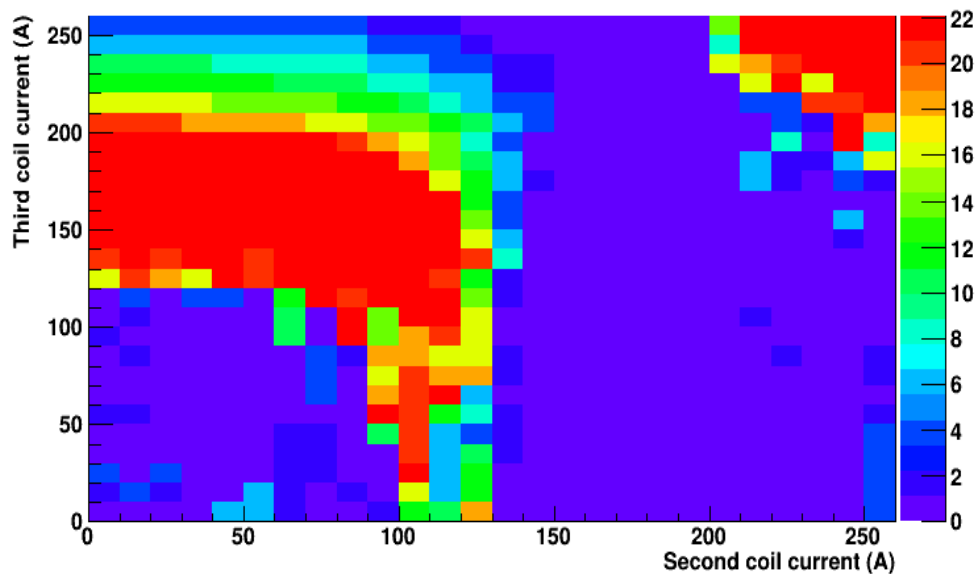
Maximum RFQ x-x' acceptance (%)



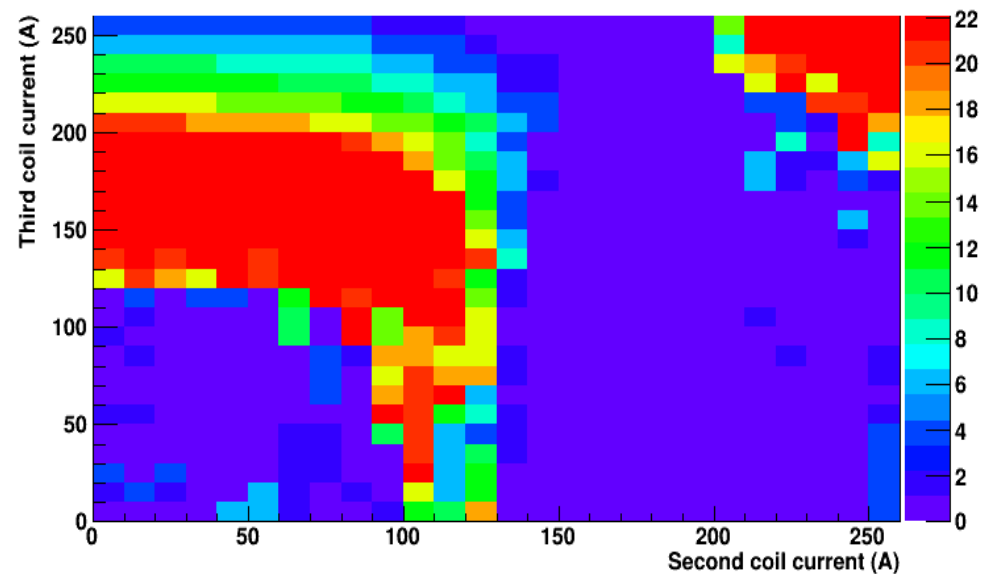
Maximum RFQ y-y' acceptance (%)



Final drift length (cm) at maximum x-x' RFQ acceptance

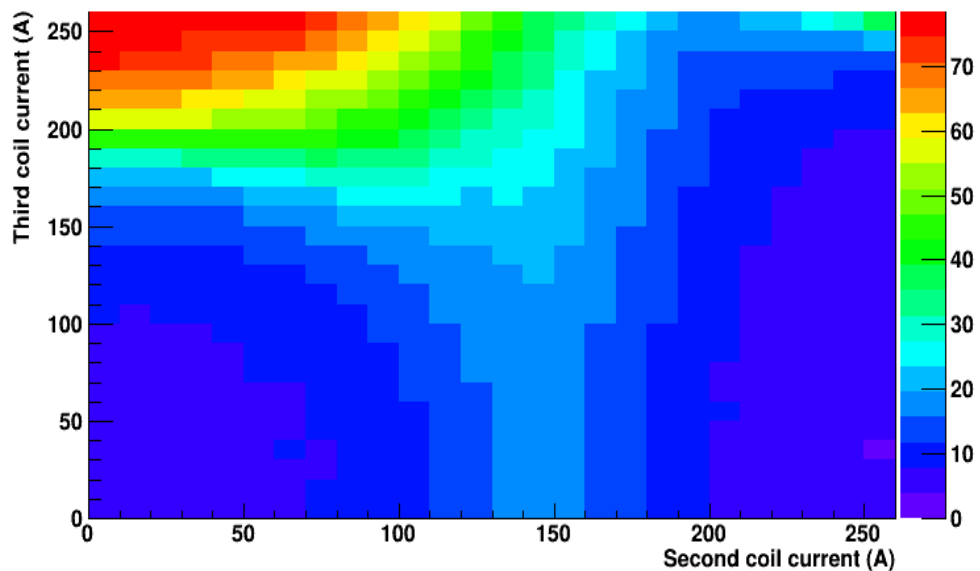


Final drift length (cm) at maximum y-y' RFQ acceptance

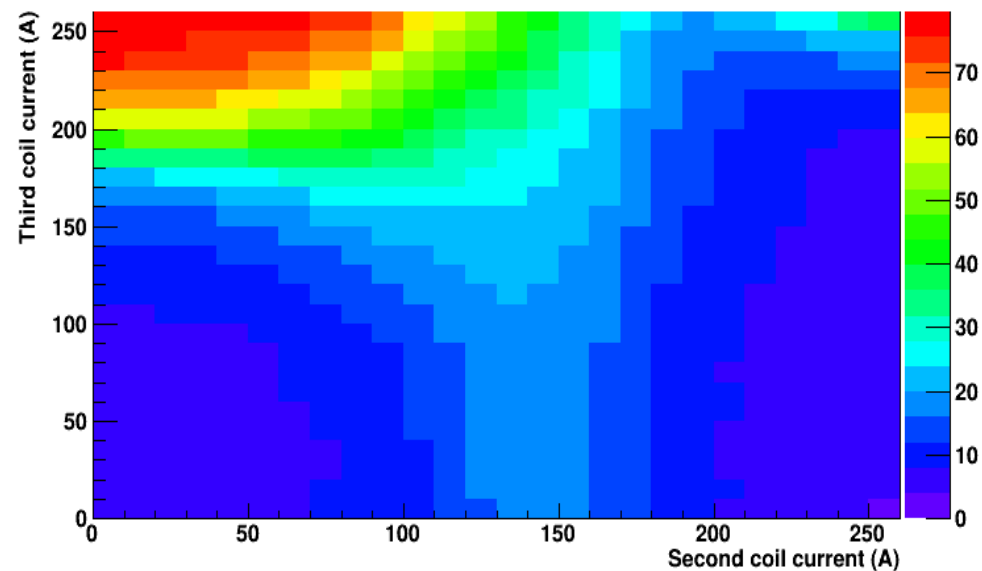


$$I_1 = 150 \text{ A}$$

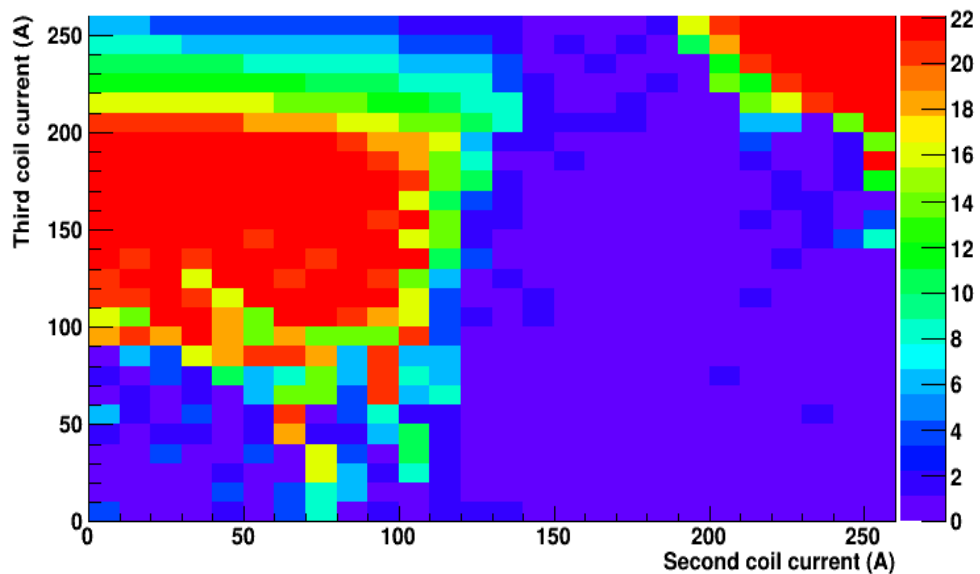
Maximum RFQ x-x' acceptance (%)



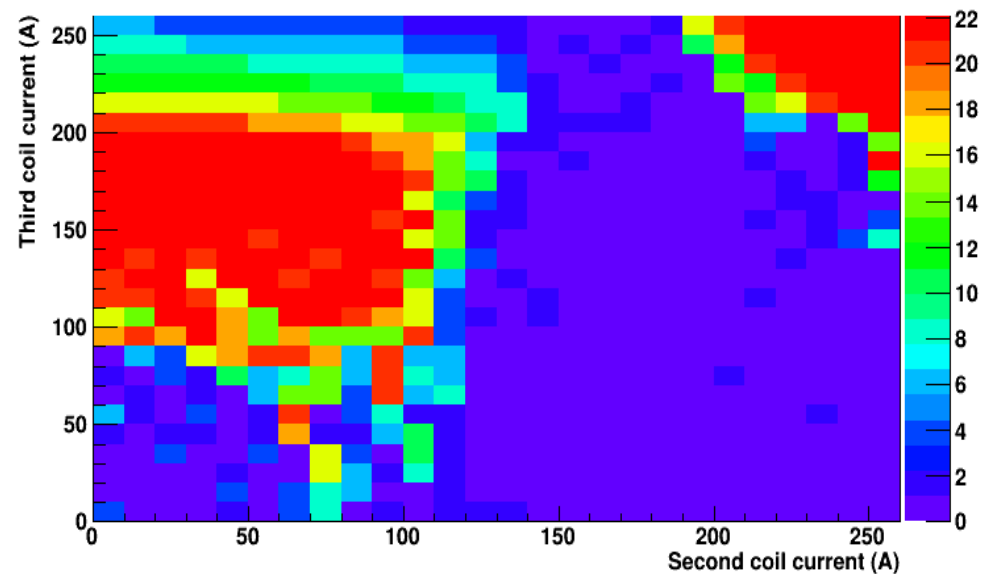
Maximum RFQ y-y' acceptance (%)



Final drift length (cm) at maximum x-x' RFQ acceptance

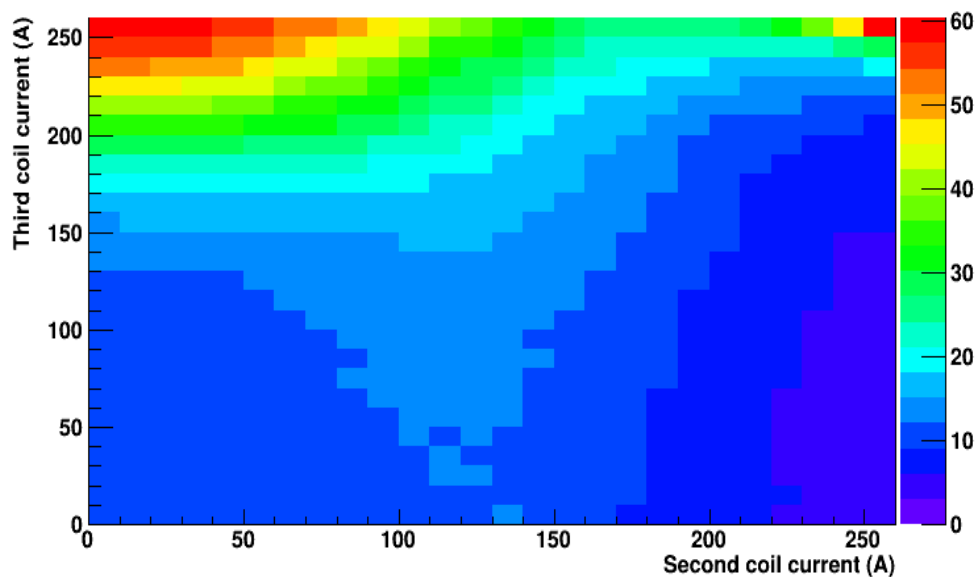


Final drift length (cm) at maximum y-y' RFQ acceptance

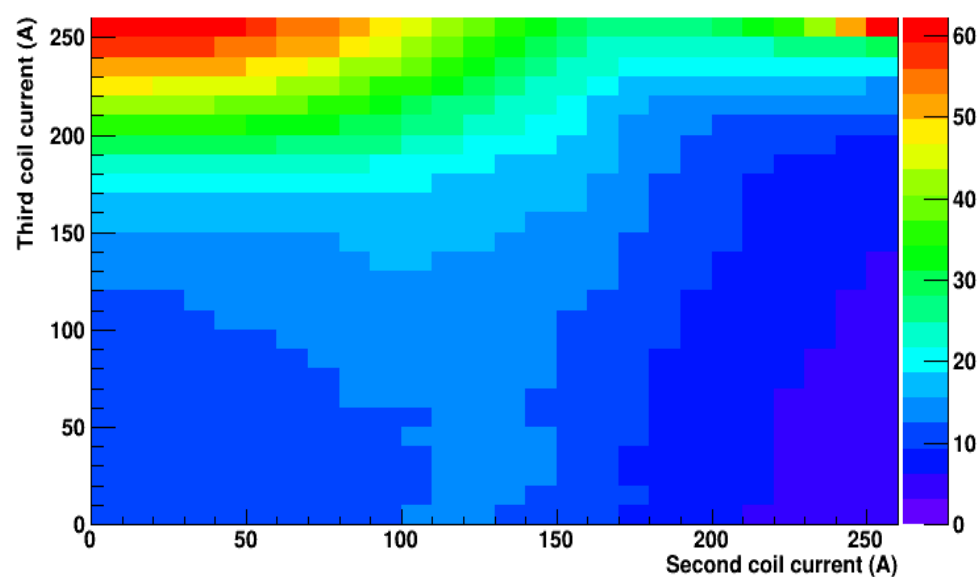


$$I_1 = 175 \text{ A}$$

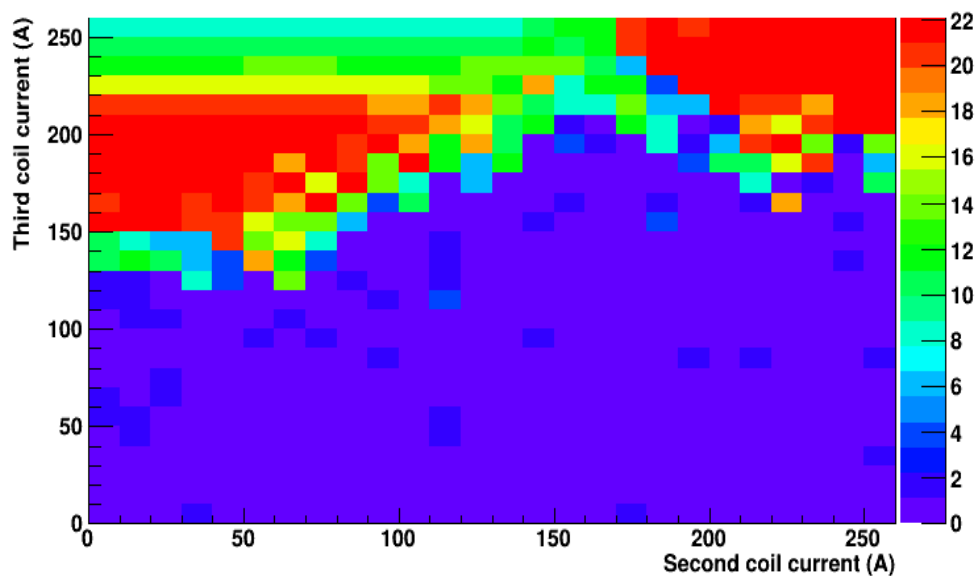
Maximum RFQ x-x' acceptance (%)



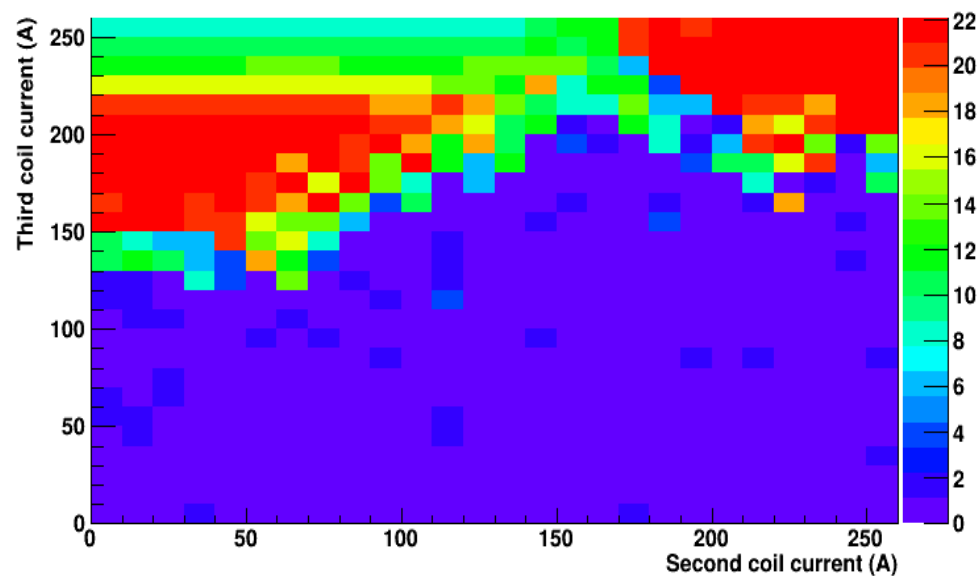
Maximum RFQ y-y' acceptance (%)



Final drift length (cm) at maximum x-x' RFQ acceptance

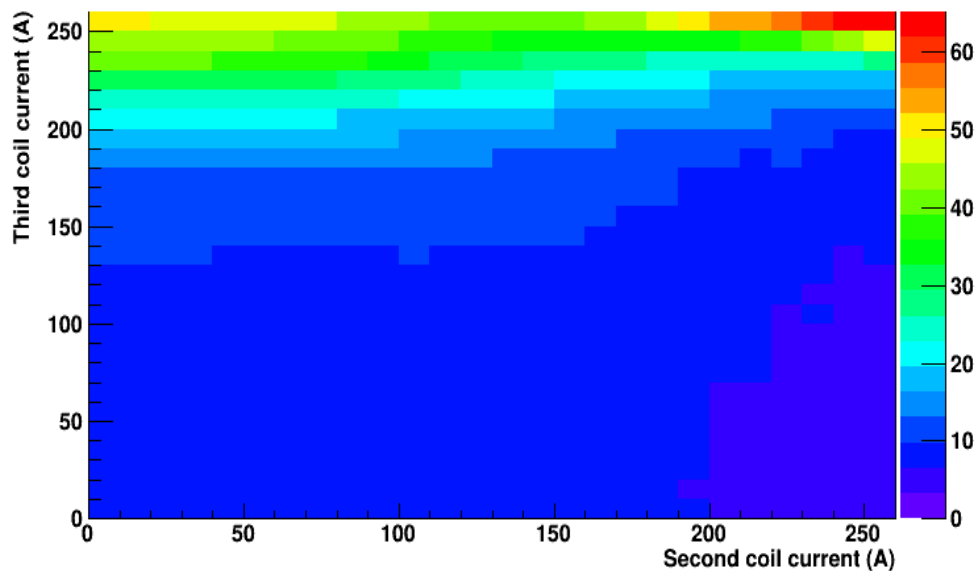


Final drift length (cm) at maximum y-y' RFQ acceptance

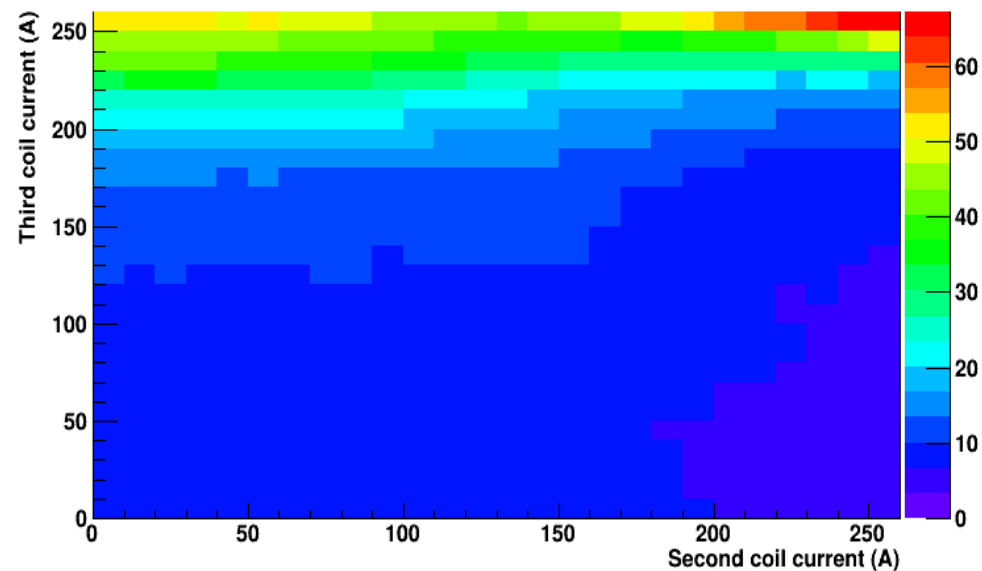


$$I_1 = 200 \text{ A}$$

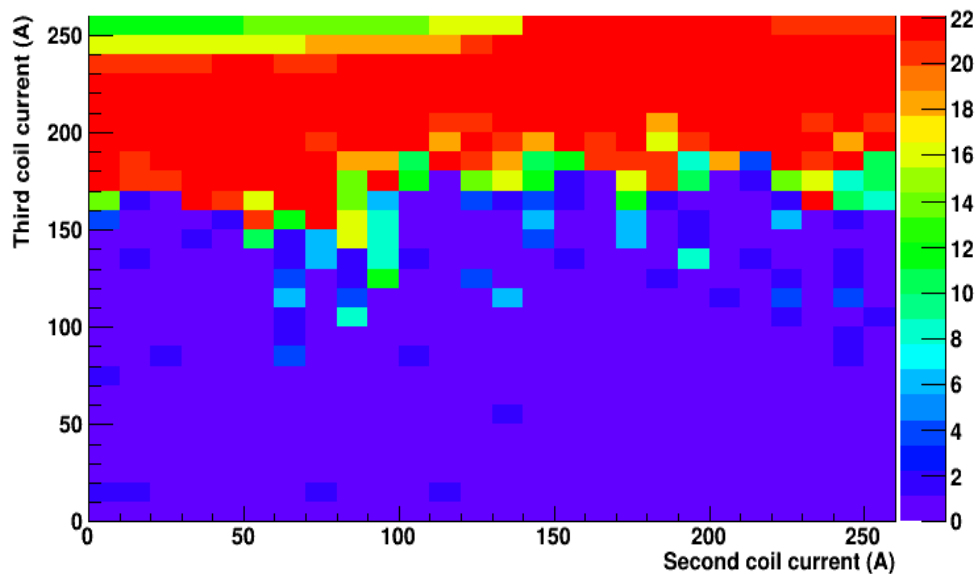
Maximum RFQ x-x' acceptance (%)



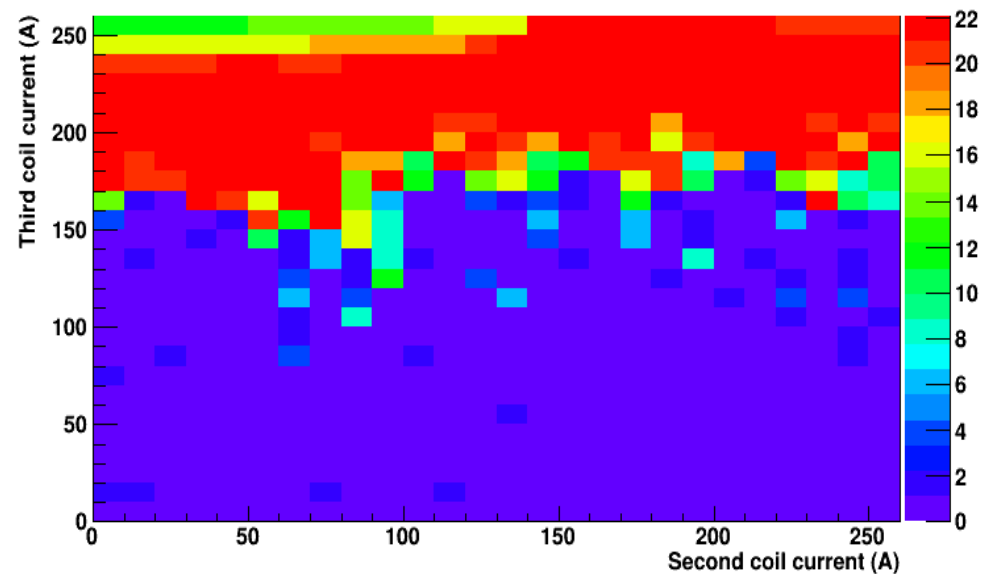
Maximum RFQ y-y' acceptance (%)



Final drift length (cm) at maximum x-x' RFQ acceptance



Final drift length (cm) at maximum y-y' RFQ acceptance



Solenoid currents range

I_1 (A)	I_2 (A)	I_3 (A)	RFQ eff (%)	Focus length (cm)
0	50 – 140	190 – 240	75 - 85	4 – >22
25	50 – 140	190 – 240	75 – 85	4 – >22
50	40 – 140	190 – 240	75 – 85	4 – >22
75	0 – 120	200 – 250	75 – 86	4 – 22
100	0 – 120	200 – 250	75 – 87	4 – 20
125	0 – 100	210 – 250	76 – 88	4 – 16
137	0 – 80	220 – 250	77 – 86	4 – 12
150	0 – 50	240 – 250	77 – 78	4 – 8
175	0 – 70	230 – 250	50 – 60	8 – 12
200	200 – 250	250	53 – 65	20 – >22

$I_1 \gtrsim 175$ A gives over-focusing of the beam inside LEBT
 \Rightarrow high I_2 & I_3 needed to focus beam again